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# Design for Assembly Line Performance: The Link Between DFA Metrics and Assembly Line Performance Metrics

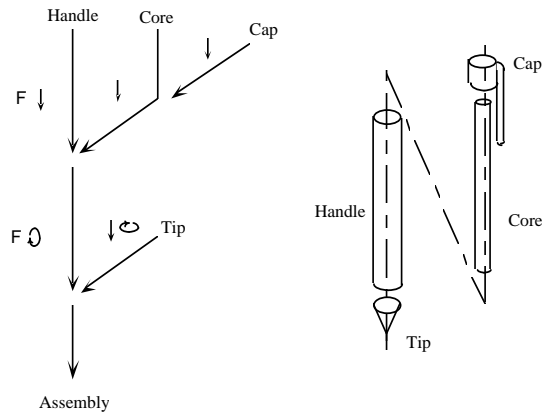
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Manufacture and Assembly



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# Motivation



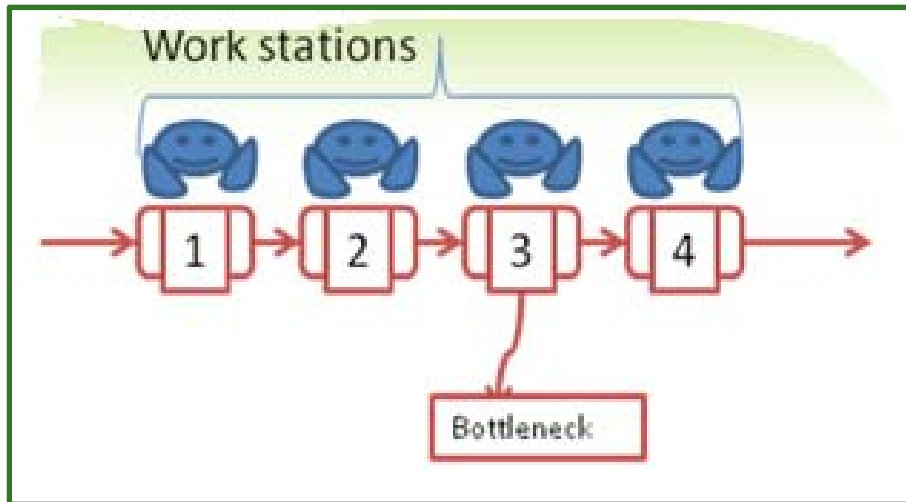
|                |               | A               | B    | C      | D       | E      | F      | G       | H       | I      | J      | K      | L      | M      | N      | O         |
|----------------|---------------|-----------------|------|--------|---------|--------|--------|---------|---------|--------|--------|--------|--------|--------|--------|-----------|
|                |               | hand.           | size | thick. | insert. | end to | inset. | insert. | insert. | fastn. | fastn. | time/  | no. of | repet. | insert | eliminate |
|                |               | cond.           |      |        | align.  | end    | direc. | cond.   | clear.  | proc   | oper.  | (T op) | (Nrep) | time   | part?  | part?     |
|                |               | 0 = no, 1 = yes |      |        |         |        |        |         |         |        |        |        |        |        |        |           |
| Part/Operation | Description   |                 |      |        |         |        |        |         |         |        |        |        |        |        |        |           |
| 1              | handle        |                 | 0.1  |        | 0.25    | 1      | 0.6    | 2.25    |         |        |        | 4.2    | 1      | 4.2    | 1      | 0         |
| 2              | Core          |                 | 0.4  |        | 0.25    | 1      | 0.6    |         | 0.25    |        | 1      | 3.5    | 1      | 3.5    | 1      | 0         |
| 3              | Cap           |                 | 0.4  |        | 0.25    | 1      | 0.6    |         | 0.9     |        | 1      | 4.15   | 1      | 4.15   | 1      | 0         |
| 4              | Flip sub-assy |                 |      |        |         |        |        | 2.25    |         |        |        | 2.25   | 1      | 2.25   | 0      | 0         |
| 5              | Tip           |                 | 0.1  |        | 0.25    | 1      | 0.6    |         | 0.25    |        | 4      | 6.2    | 1      | 6.2    | 1      | 0         |
| 6              |               |                 |      |        |         |        |        |         |         |        |        |        |        |        |        |           |
| 7              |               |                 |      |        |         |        |        |         |         |        |        |        |        |        |        |           |
| 8              |               |                 |      |        |         |        |        |         |         |        |        |        |        |        |        |           |
| 9              |               |                 |      |        |         |        |        |         |         |        |        |        |        |        |        |           |
| ##             |               |                 |      |        |         |        |        |         |         |        |        |        |        |        |        |           |
|                |               |                 |      |        |         |        |        |         |         |        |        |        | 5      | 20.3   | 4      |           |
|                |               |                 |      |        |         |        |        |         |         |        |        |        | TOP    | TAT    | NUP    |           |

## Summary Statistics

|      |       |                                      |
|------|-------|--------------------------------------|
| NUP  | 4     | = number of unique parts             |
| TOP  | 5     | = total no. of operations            |
| TAT  | 20.3  | = total assembly time                |
| NP   | 4     | = no. of parts = sumprod.(L,N)       |
| Tavg | 4.06  | = avg time/operation = TAT/(sumRep)  |
| Pmin | 4.0   | = min # parts = NP - sumprod.(L,N,O) |
| AR   | 0.463 | = Assembly rating = 2.35 * NP /TAT   |
| PE   | 1     | = Part Efficiency = Pmin/NP          |

- Fewer Parts
- Easier Assembly
- Shorter Assembly Time
  - Major Cost Savings
  - Reduced Defects
  - Improved Quality & Reliability

# Motivation



- Cycle Time
- Work in Process
- Line Balancing

***Typically Performed After Design Has Been Completed***

***Can these metrics be linked to the design stage, so that improvements to manufacturing line performance can be made through design changes?***

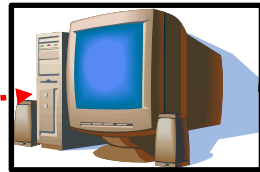
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# Original Research Questions

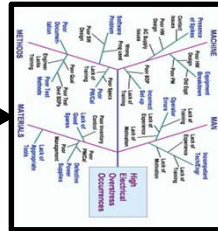
- Can an explicit link between DFA and assembly line performance be made?
  - If so, can this link be leveraged to provide a method to aid product development practitioners during product development?
  - What type of design actions can be taken to improve manufacturing line performance given an initial design candidate?
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# Methodology

## Design Analysis



Representation of Design Candidate



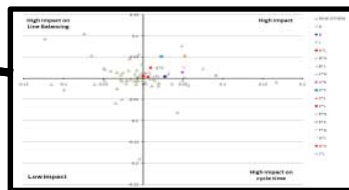
ASSEMBLY FISHBONE

A table titled 'DFA ANALYSIS' showing a detailed breakdown of design features and their manufacturability. The table has columns for 'Design Features', 'Manufacturability', and 'DFA Score'.

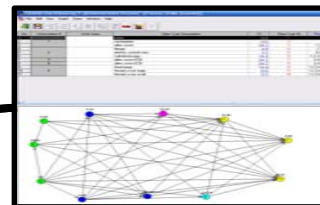
| Design Features          | Manufacturability | DFA Score |
|--------------------------|-------------------|-----------|
| Assembly                 | High              | 9.5       |
| Fasteners                | Medium            | 7.5       |
| Welds                    | Low               | 5.5       |
| Subassemblies            | High              | 9.5       |
| Complexity               | Medium            | 7.5       |
| Material                 | High              | 9.5       |
| Surface Finish           | Medium            | 7.5       |
| Dimensional Accuracy     | High              | 9.5       |
| Assembly Sequence        | High              | 9.5       |
| Assembly Time            | High              | 9.5       |
| Assembly Cost            | High              | 9.5       |
| Assembly Safety          | High              | 9.5       |
| Assembly Reliability     | High              | 9.5       |
| Assembly Maintainability | High              | 9.5       |
| Assembly Flexibility     | High              | 9.5       |
| Assembly Scalability     | High              | 9.5       |
| Assembly Sustainability  | High              | 9.5       |

DFA ANALYSIS

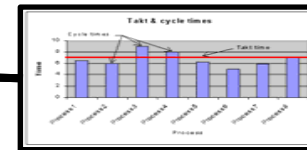
## Manufacturing Performance Analysis



Redesign Action

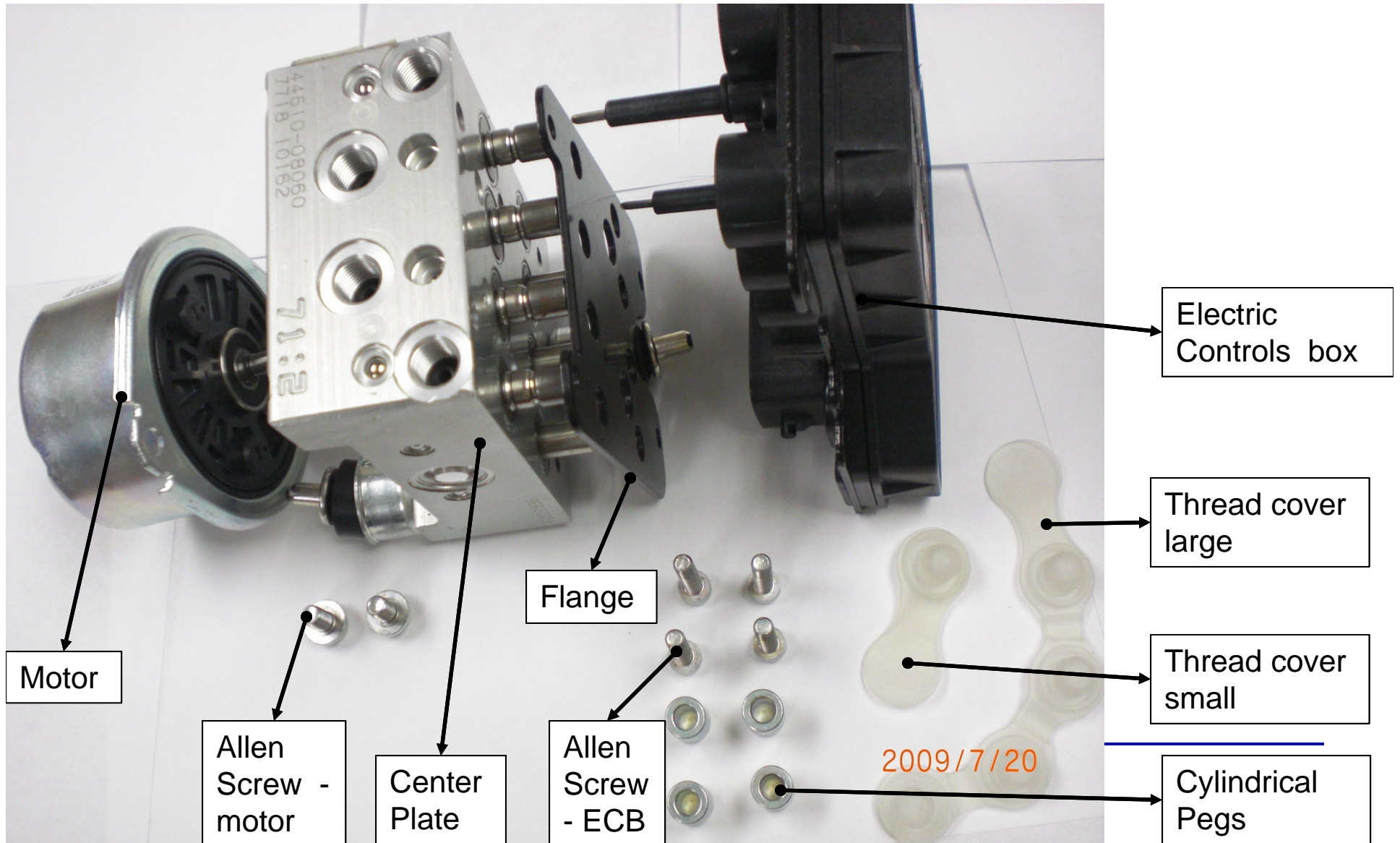


Relaxing precedence



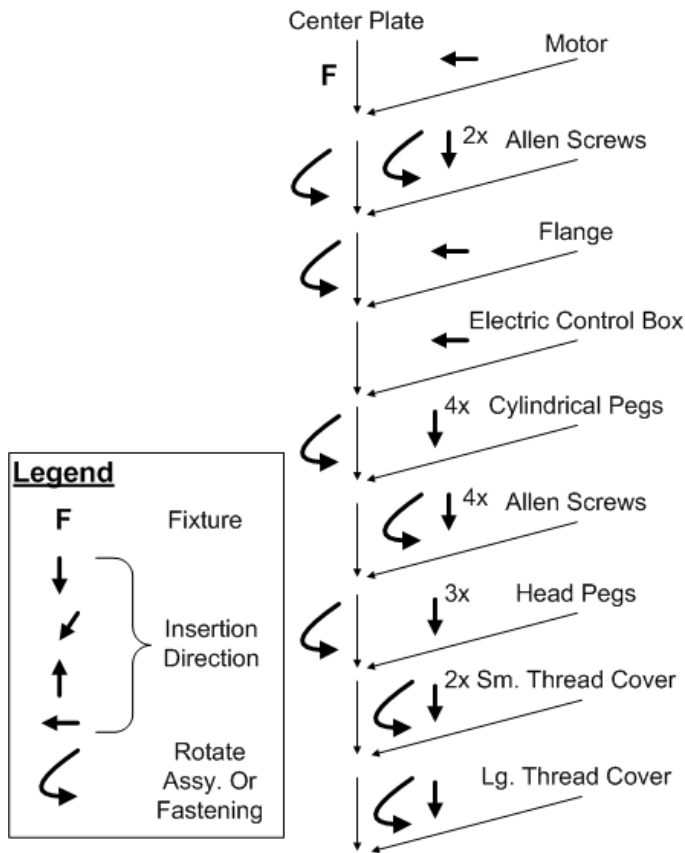
Manufacturing Analysis

# Design Analysis: Select Design Candidate





# Design Analysis: DFA



|    |                            | Time Factors (seconds) |                      |           |                |                     |                     |                     |           |                   |                    |  |   |   |                               |                                  |
|----|----------------------------|------------------------|----------------------|-----------|----------------|---------------------|---------------------|---------------------|-----------|-------------------|--------------------|--|---|---|-------------------------------|----------------------------------|
|    |                            | A                      | B                    | C         | D              | E                   | F                   | G                   | H         | I                 | J                  | K                                      | L   | M   | N                             | O                                |
|    |                            | End-to-End Orientation | Rotational Alignment | Part Size | Part Thickness | Insertion Clearance | Insertion Direction | Insertion Condition | Fastening | Fastening Process | Handling Condition | Time/Each Operation (T <sub>op</sub> ) | Number of Repetitions (N <sup>rep</sup> ) | Repetition Time (K*L) (T <sup>rep</sup> ) | Insert Part (1 = Yes; 0 = No) | Eliminate Part (1 = Yes; 0 = No) |
| No | Part/Operation Description |                        |                      |           |                |                     |                     |                     |           |                   |                    |  |   |   |                               |                                  |
| 1  | Motor                      | 0.8                    | 1.5                  | 0.0       | 0.0            | 1.6                 | 1.4                 | 1.3                 | 0.0       | 0.0               | 0.0                | 6.6                                    | 1   | 6.6                                       | 1                             |                                  |
| 2  | Center Plate               | 0.0                    | 0.5                  | 0.0       | 0.0            | 0.0                 | 0.0                 | 0.0                 | 0.0       | 0.0               | 0.0                | 0.5                                    | 1   | 0.5                                       | 1                             |                                  |
| 3  | Flange                     | 2.3                    | 1.0                  | 0.0       | 0.2            | 0.0                 | 1.4                 | 0.0                 | 0.0       | 0.0               | 0.0                | 4.9                                    | 1   | 4.9                                       |                               |                                  |
| 4  | Electric controls box      | 0.8                    | 1.0                  | 0.0       | 0.0            | 0.0                 | 1.4                 | 0.0                 | 0.0       | 0.0               | 0.0                | 3.2                                    | 1   | 3.2                                       | 1                             |                                  |
| 5  | head pegs                  | 0.8                    | 0.5                  | 0.1       | 0.0            | 0.9                 | 0.6                 | 0.0                 | 1.0       | 1.0               | 0.0                | 4.8                                    | 3   | 14.4                                      |                               |                                  |
| 6  | allen screw                | 1.8                    | 0.0                  | 0.1       | 0.0            | 0.3                 | 0.6                 | 1.3                 | 4.0       | 4.0               | 0.0                | 12.1                                   | 4   | 48.4                                      |                               |                                  |
| 7  | allen screw motor          | 1.8                    | 0.0                  | 0.1       | 0.0            | 0.3                 | 0.6                 | 1.3                 | 4.0       | 4.0               | 0.0                | 12.1                                   | 2   | 24.2                                      |                               |                                  |
| 8  | thread cover small         | 1                      | 1                    | 0         | 0              | 0                   | 1                   | 0                   | 1         | 1                 | 0                  | 4.6                                    | 2   | 9.2                                       |                               |                                  |
| 9  | cylindrical pegs           | 1                      | 0                    | 0         | 0              | 0                   | 1                   | 1                   | 0         | 0                 | 0                  | 3.6                                    | 4   | 14.4                                      |                               |                                  |
| 10 | thread cover large         | 1                      | 0                    | 0         | 0              | 0                   | 1                   | 0                   | 1         | 4                 | 0                  | 6.6                                    | 1   | 6.6                                       |                               |                                  |
|    |                            |                        |                      |           |                |                     |                     |                     |           |                   |                    | 20                                     | 132.4                                     | 3   |                               |                                  |
|    |                            |                        |                      |           |                |                     |                     |                     |           |                   |                    | TOP                                    | TAT                                       | NUP                                       |                               |                                  |

| Step    | Description   | Parameter        | Value | Formula  |
|---------|---|------------------|-------|--|
| Step 1: | Draw the Assembly Sequence Diagram                          |                  |       |  |
| Step 2: | List Parts & operations in order (left column)              |                  |       |  |
| Step 3: | Enter times from Estimated DFA Time Chart                   |                  |       |  |
| Step 4: | Sum time per part/oper. in column K                         |                  |       |  |
|         | Enter no. of repetitions for each operation in col. L       |                  |       |  |
|         | Enter K*L in col. M   |                  |       |  |
| Step 5: | Enter a 1 in col. N if a part was inserted during operation |                  |       |  |
|         | Enter a 1 in col. O if part or operation can be eliminated  |                  |       |  |
| Step 6: | Calculate Summary Statistics                                |                  |       |  |
|         |   | NUP              | 3     | = number of unique parts (Sum of Column N)     |
|         |   | TOP              | 20    | = total number of operations (sum of Column L) |
|         |   | TAT              | 132.4 | = total assembly time (sum of Column M)        |
|         |   | NP               | 3     | = number of parts = sumproduct(L,N)            |
|         |   | T <sub>avg</sub> | 6.6   | = avg time/operation = TAT/TOP                 |
|         |   | P <sub>min</sub> | 3.0   | = min # parts = NP - sumproduct(L,N,O)         |
|         |   | AR               | 0.05  | = Assembly rating = 2.35 * NP / TAT            |
|         |   | PE               | 1.00  | = Part Efficiency = Pmin/NP                    |
|         |   | C                | 84.40 | = Assembly complexity = TAT - (2.4*TOP)        |
|         |   | OR               | 2.76  | = Operation difficulty rating = TAT/(2.4*TOP)  |

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# Manufacturing Performance Analysis

- Determine Baseline

- Inputs

- Candidate design precedence relationships, TAKT Time

- COMSOAL Algorithm selected

- Ease of implementation

- Relevant Outputs

- Number of Workstations, Cycle Time, Recommended Assembly Sequence

- Identify Components Most Likely to Improve Manufacturing Line Performance

- Systematically (& Artificially) Relax Precedence Constraints

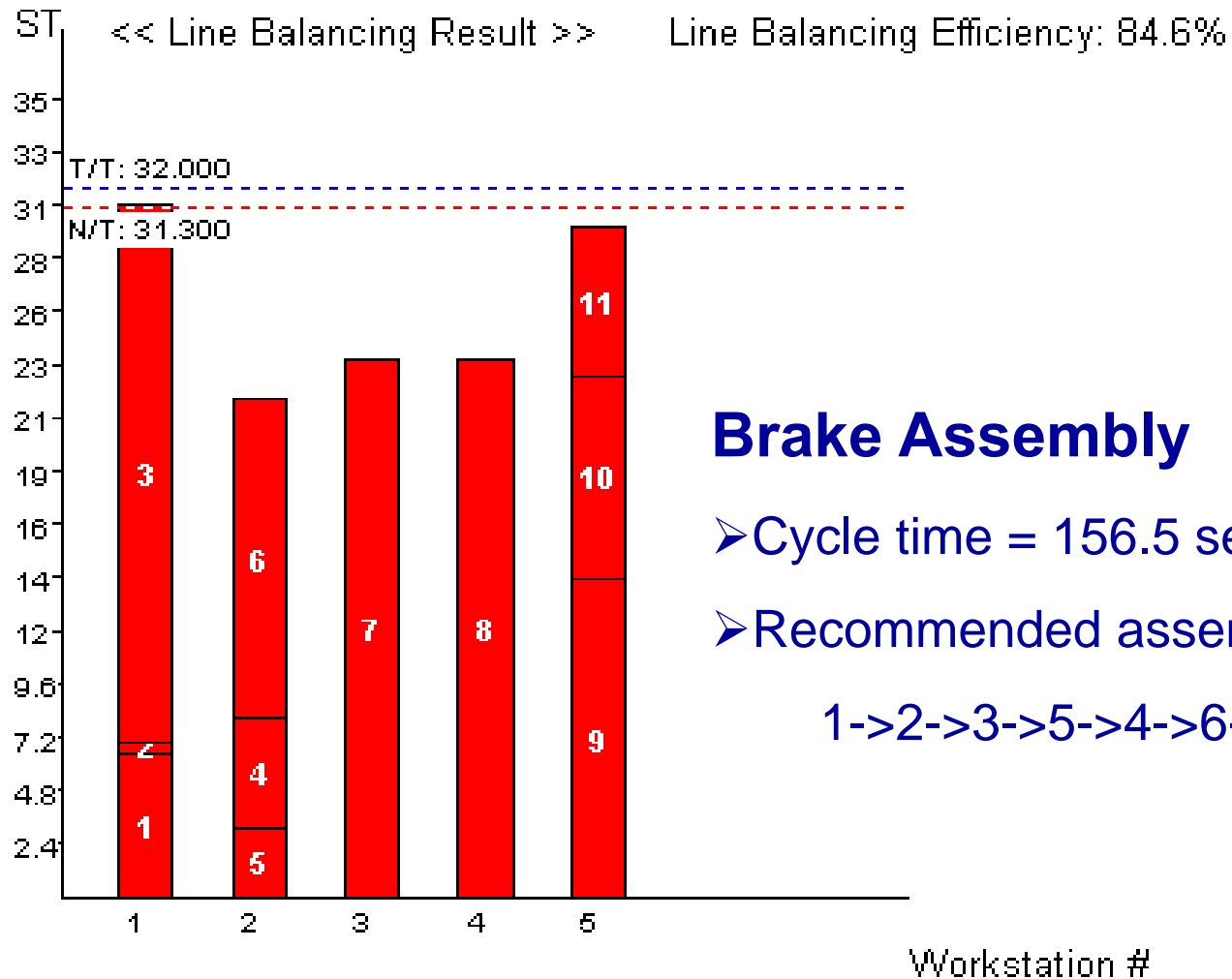
- Select Components with Biggest Performance Indices Change

- Redesign Actions

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# Determine Baseline



# Performance Improvement Indices

## ■ Cycle Time Index

$$CTI = \left(1 - \left(\frac{CT_p}{CT_{Baseline}}\right)\right)$$

where,

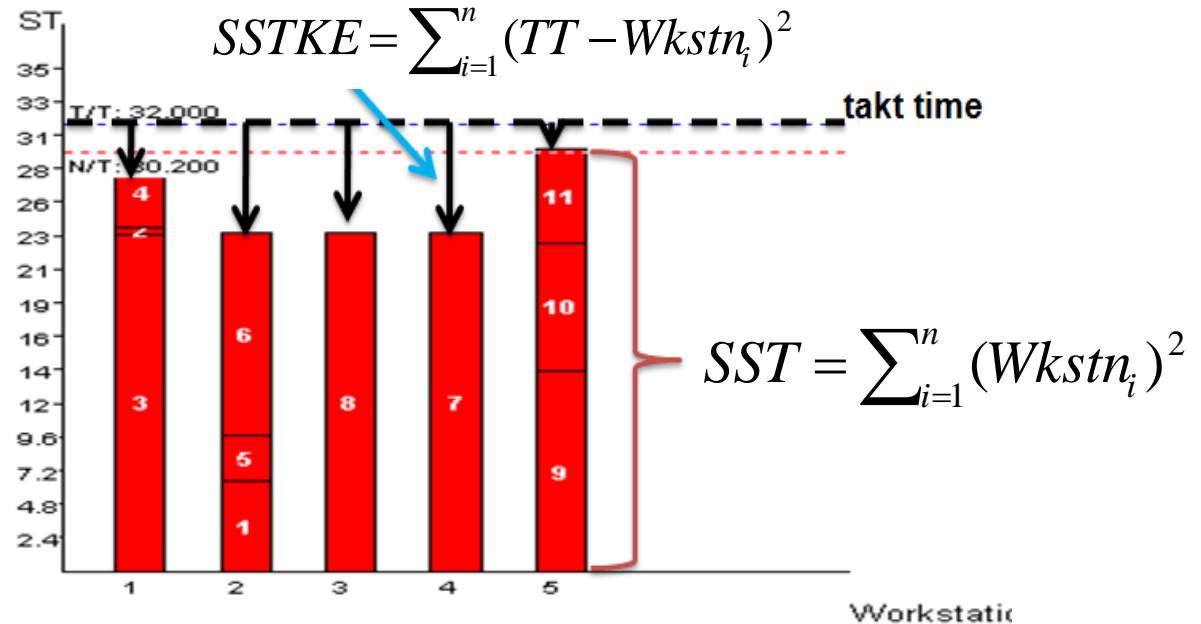
CTI = Cycle Time Index  
 CT<sub>p</sub> = Cycle time of a permutation

CT<sub>Baseline</sub> = Cycle time of a line considering all components in the original design

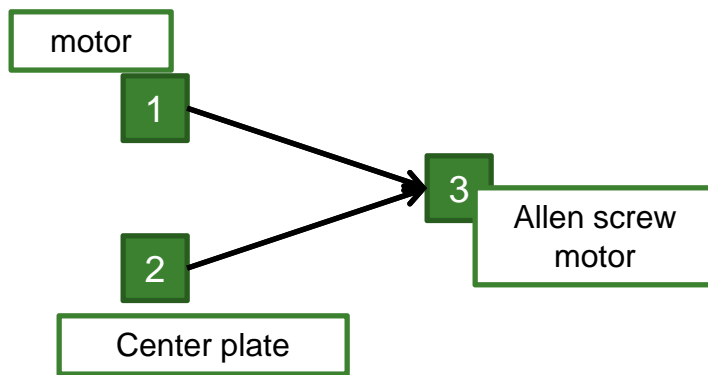
## ■ Line Balancing Index

$$LBI = 1 - \frac{SSTKE}{SST}$$

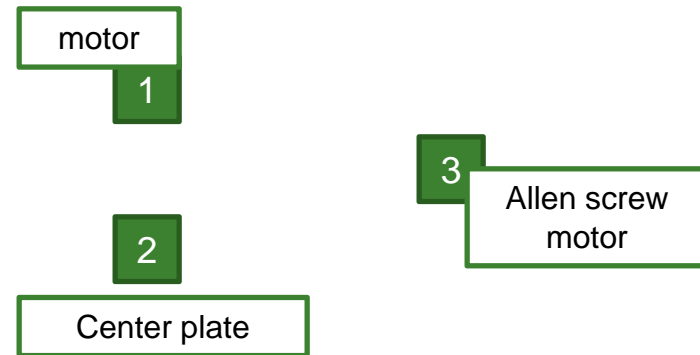
$$SSTKE = \sum_{i=1}^n (TT - Wkstn_i)^2$$



# Relaxing Precedence Relationships



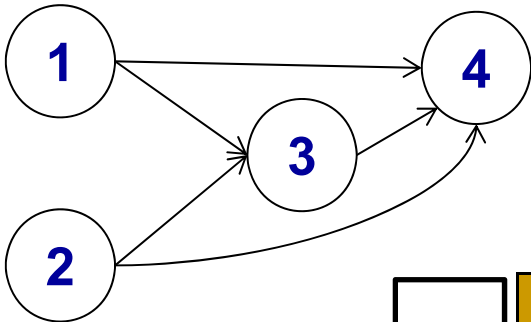
**Allen screw with precedence constraints**



**Allen screw without precedence constraints**

- The feasible assembly sequences with precedence:
  - 1->2->3 or 2->1->3
- The feasible assembly sequences *without* precedence:
  - 1->2->3 or 1->3->2 or 2->1->3 or 2->3->1 or 3->2->1 or 3->1->2

# Systematically Relaxing Precedence Relationships



**SUPPLYING**

| <b>RECEIVING</b> | COMPONENT | 1                  | 2 | 3               | 4 |
|------------------|-----------|--------------------|---|-----------------|---|
|                  | 1         |                    |   |                 |   |
|                  | 2         | Column Permutation |   |                 |   |
|                  | 3         | ○                  | ○ | Row Permutation |   |
|                  | 4         | ○                  | ○ | ○               |   |

# Systematically Relaxing Precedence Relationships

Minitab - ROW PERMUTATIONS.MPJ - [Worksheet 1 \*\*\*]

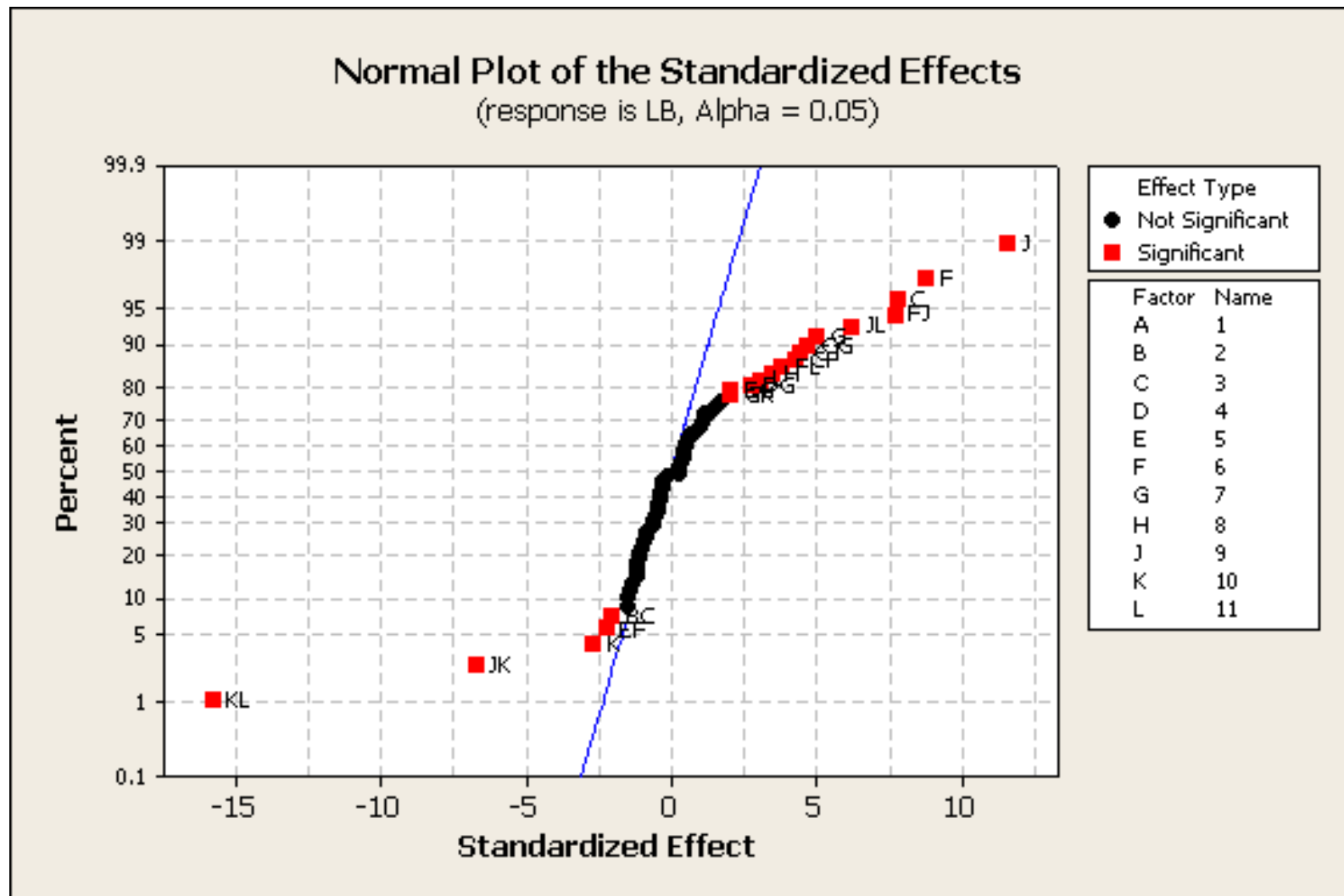
File Edit Data Calc Stat Graph Editor Tools Window Help

CTI & LBI Calculated for Each Configuration

|    | C1 | C2 | C3 | C4 | C5 | C6 | C7 | C8 | C9 | C10 | C11 | C12     | C13      |
|----|----|----|----|----|----|----|----|----|----|-----|-----|---------|----------|
|    | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10  | 11  | CTI     | LBI      |
| 1  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0   | 0   | 0.35144 | 0.162071 |
| 2  | 1  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0   | 0   | 0.79872 | 0.145403 |
| 3  | 0  | 1  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0   | 0   | 0.79872 | 0.145403 |
| 4  | 1  | 1  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0   | 0   | 0.79872 | 0.145403 |
| 5  | 0  | 0  | 1  | 0  | 0  | 0  | 0  | 0  | 0  | 0   | 0   | 0.35144 | 0.162071 |
| 6  | 1  | 0  | 1  | 0  | 0  | 0  | 0  | 0  | 0  | 0   | 0   | 0.35144 | 0.162071 |
| 7  | 0  | 1  | 1  | 0  | 0  | 0  | 0  | 0  | 0  | 0   | 0   | 0.35144 | 0.162071 |
| 8  | 1  | 1  | 1  | 0  | 0  | 0  | 0  | 0  | 0  | 0   | 0   | 0.35144 | 0.162071 |
| 9  | 0  | 0  | 0  | 1  | 0  | 0  | 0  | 0  | 0  | 0   | 0   | 0.79872 | 0.145403 |
| 10 | 1  | 0  | 0  | 1  | 0  | 0  | 0  | 0  | 0  | 0   | 0   | 0.79872 | 0.145403 |
| 11 | 0  | 1  | 0  | 1  | 0  | 0  | 0  | 0  | 0  | 0   | 0   | 0.19169 | 0.162951 |

$2^{11}$  Possible Combination of Relaxed Constraint Configurations

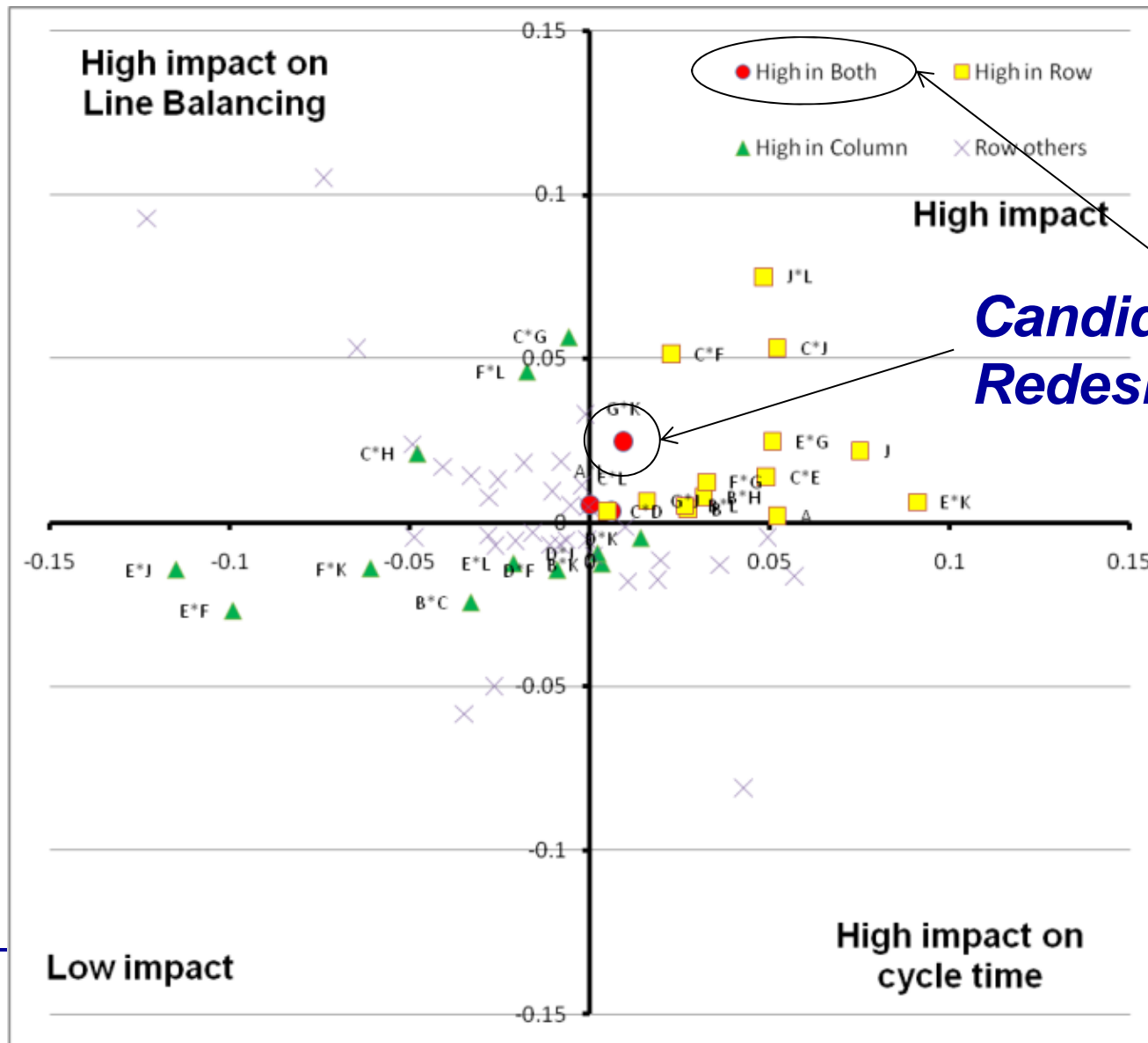
# Filtering the Data



Brake Assembly: Significant effects plot (Row Permutation)



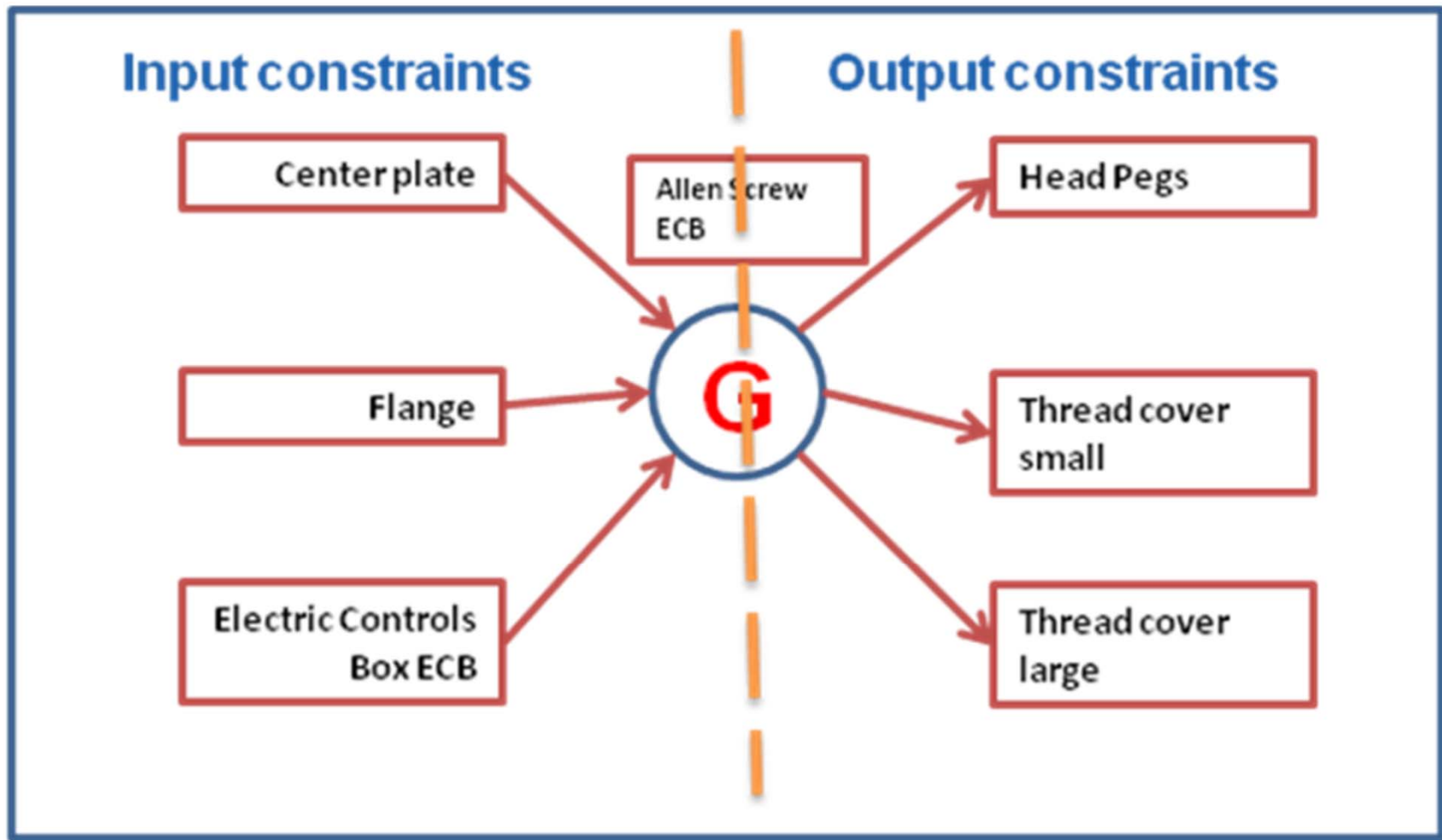
# Identifying Components for Redesign



# Redesign Actions (Adapted from Whitney, 2004)

| Symbol | Constraint           | Interpretation  | Analysis            | Recommendations   |
|--------|----------------------|---|---------------------|---|
| U      | Under-constrained    | Degree of freedom has no value and it is required or necessary      | Motion Analysis     | Redesign or combine components for making the assembly properly constrained   |
| O      | Over-constrained     | Degree of freedom has more than one value creating locked in stress | Constraint analysis | Redesign or eliminate the component for making the assembly properly constrained  |
| P      | Properly Constrained | The part is neither over constrained nor under constrained          | not required        | If all constraints are properly constrained then analyze the assembly of the part and the mating parts as a whole for opportunities of redesign |
| M      | Mistake              | Non functional over constraint or under constraint                  | not required        | Eliminate   |

# Redesign Actions



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# Conclusions

- Link between DFA and assembly line performance established
- Analysis procedure developed to systematically identify redesign components
  - line balance and cycle time performance could be improved during the design stage
- Potential utility of the approach demonstrated through a case study

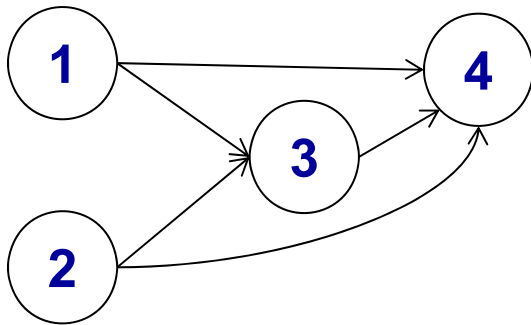
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# Opportunities to Explore

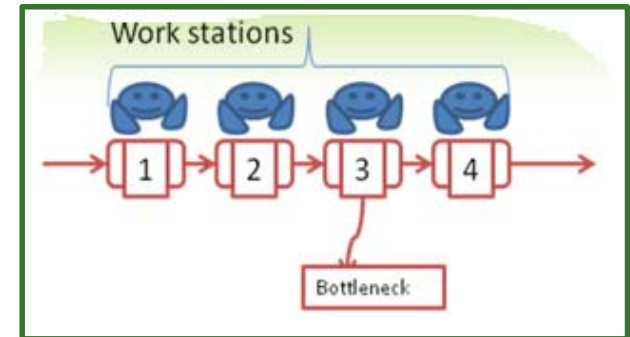
- The use of a more efficient and effective line balancing algorithm
  - A more efficient and effective search process to identify redesign candidates
  - More systematic guidance on redesign actions based on the analysis results
  - The validation of the methodology on more realistic case studies.
-

# Line Balancing

Thangavelu and Shetty, 1971



**Set of Tasks**  
 $i=\{1,2,3..n\}$



**Set of Workstations**  
 $j=\{1,2,3..n\}$

$$Min\_Z = \sum_{i=1}^n \sum_{j=1}^n C_j X_{ij}$$

$nC_j \leq C_{j+1}$

1, if task i assigned to station j  
 0, otherwise

- Each task is assigned to only one station
- Time for processing all tasks assigned to each station does not exceed the takt time
- Precedence constraints are preserved
- Any task is assigned to a station only if all its predecessors have been already assigned to a previously opened station, or to the same station

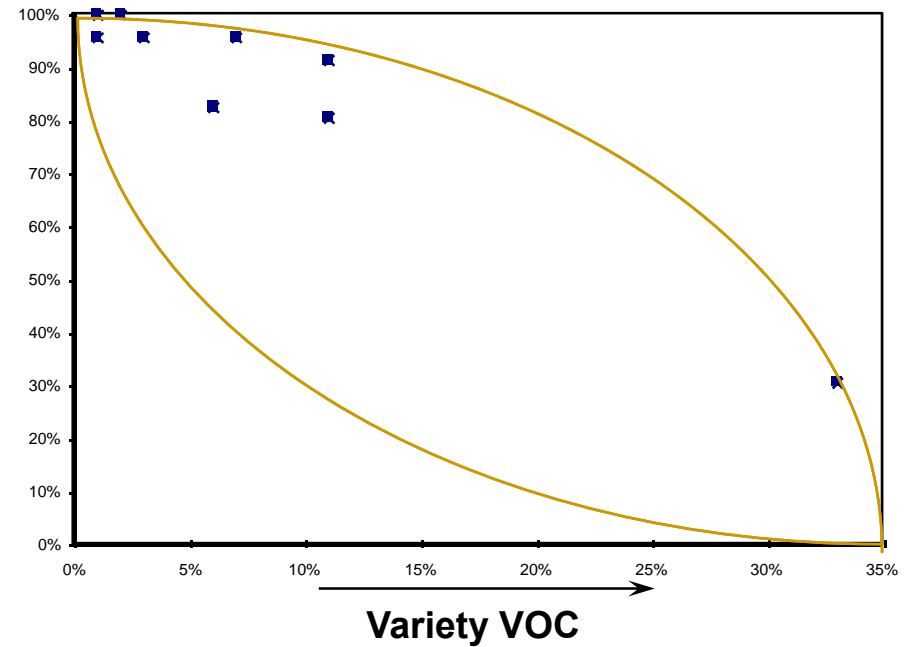
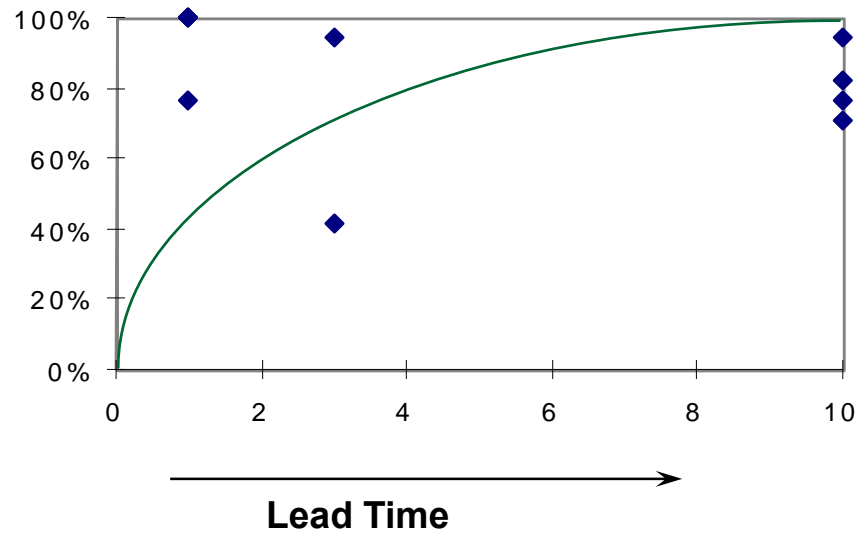
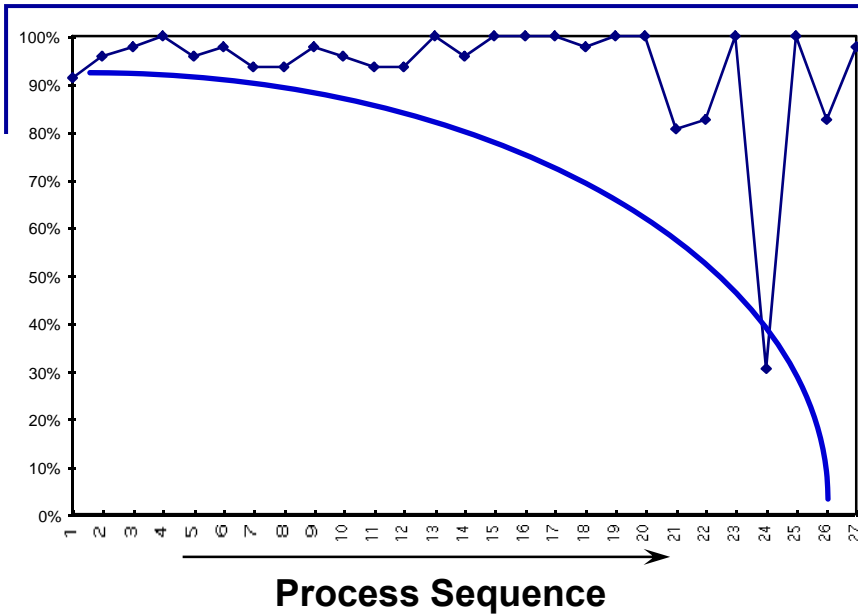


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# Design Candidate Search

- How do we efficiently and effectively identify the precedence constraints that should be explored for elimination (by taking a redesign action)?
  - How do we efficiently and effectively identify assembly tasks that should be split-up (also through redesign action)?
-

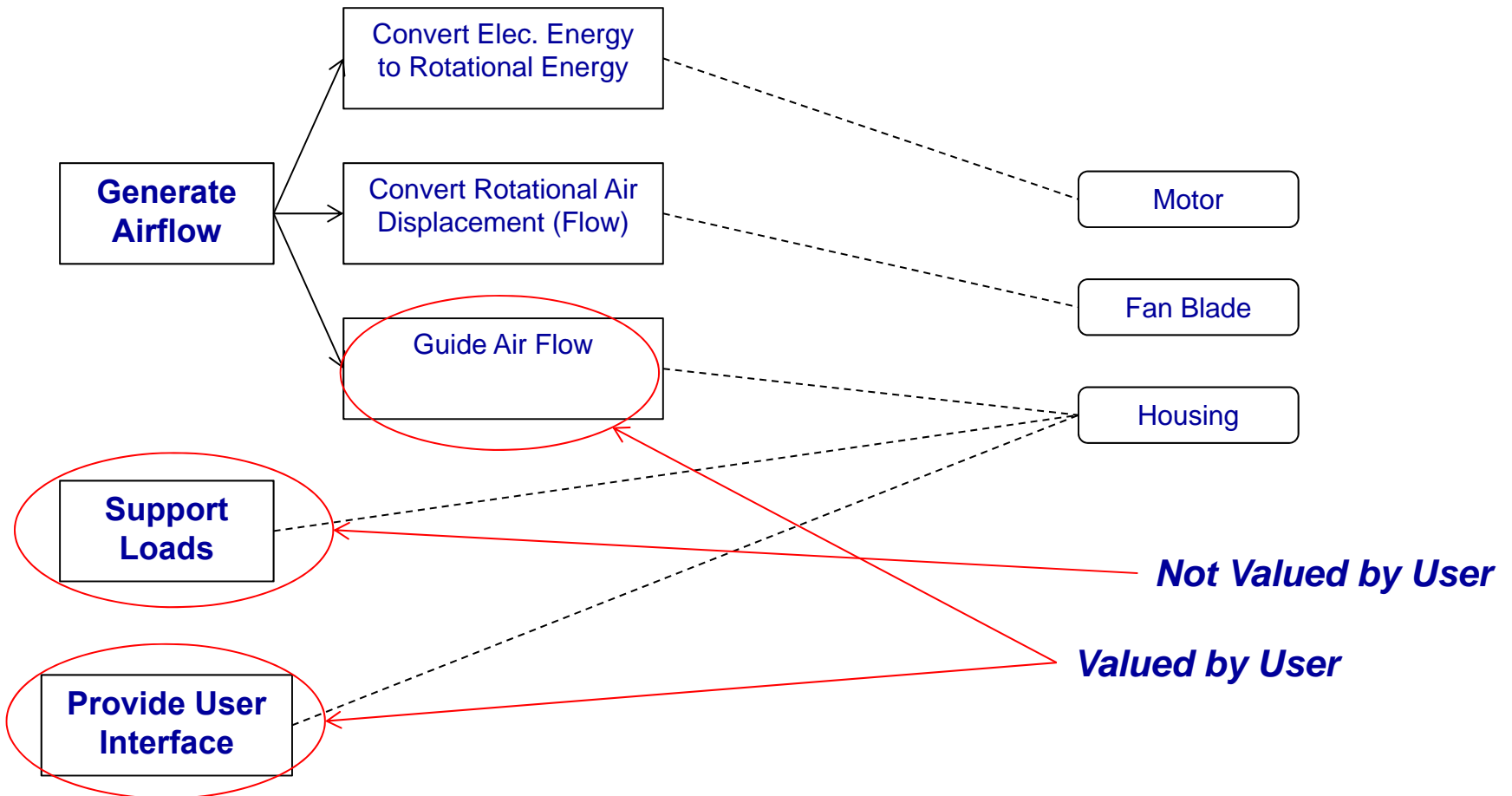
# Design for Variety



# Component Division

## Functions

## Components



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# Next Steps

- Develop Metrics as Discussed Above
  - Integrate into an optimization problem formulation
    - May result in non-linear formulations
    - Linearization or other techniques may be necessary to solve
  - Identify Industry Partner to develop realistic case study
    - Essential to elicit implementation issues & to demonstrate utility
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# Questions

